



## End Semester Examination – Nov/Dec – 2016

Code : **14EI3005**  
Sub. Name : **Advanced control system**

Semester : **2016-17 ODD**  
Duration : **3hrs**  
Max. marks : **100**

### ANSWER ALL QUESTIONS (5 x 20 = 100 Marks)

Q. No.	Sub Div.	Questions	Course Outcome	Marks
1.	a.	Consider the mechanical system given below. Model the system and derive the transfer function in terms of $X_3(s)$ and $F(s)$	CO1	15
	b.	What are the essential elements of control systems	CO1	5
(OR)				
2.	a.	Write the steps involved in mathematical model of a process.	CO1	5
	b.	Obtain the mathematical model in state space of a permanent magnet stepper motor from its principles.	CO1	15
3.	a.	Solve the equation $\frac{dy}{dx} = 1 - y$ with the initial condition $x = 0, y = 0$ using modified Euler's method and tabulate the solutions at $x = 0.1, 0.2$ and $0.3$ . Compare the result with the results of the exact solution	CO2	10
	b.	Find $y(0.1)$ by Taylor series method if $y' = x^2y - 1$ ; $y(0) = 1$ .	CO2	10
(OR)				
4.	a.	Consider $u^1 = -2tu^2$ where $u(0)=1$ with $h=0.2$ on the interval $[0,0.6]$ . Solve the initial value problem given above. Use 4 <sup>th</sup> order RK method.	CO3	20
5.	a.	Give a short note on the relationship between controllability and observability.	CO2	5
	b.	The state model of a system is	CO3	15
		$\begin{pmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 1 \\ -2 & -3 & 0 \\ 0 & 2 & -3 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} + \begin{pmatrix} 0 \\ 2 \\ 0 \end{pmatrix} [u]$		
		Convert the state model to controllable phase variable form		
(OR)				
6.	a.	Solve the given differential equation using Taylor series.	CO2	12
		$\frac{d^2x}{dt^2} + 3\frac{dx}{dt} + 6tx = 0$ ; While its initial conditions are $x(0) = 1$ and $\frac{dx(0)}{dt} = 1$		

	b.	Write short notes on phase planes and phase trajectories.	CO1	4
	c.	Briefly explain principle of linearization.	CO1	4
7.	a.	Define the terms controllability and observability.	CO3	
	b.	A single-input system is described by the following state equation $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 \\ 1 & -2 & 0 \\ 2 & 1 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 10 \\ 1 \\ 0 \end{bmatrix} u$ Design a state feedback controller which will give closed-loop poles at $-1+j2, -1-j2, -6$ .	CO2	20
<b>(OR)</b>				
8.	a.	1. Consider the system defined by: $\dot{x} = Ax + Bu$ Where $A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -5 & -6 \end{bmatrix}, B = \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}$ By using state-feedback control $u = -Kx$ , it is desired to have the closed-loop poles at $s = -2 \pm j4, s = -10$ . Determine the state-feedback gain matrix $K$ .	CO2	15
	b.	Consider a system $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} -5 & 2 & 1 \\ 0 & 0 & 1 \\ -1 & -4 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u$ Output: $y = x_1$ Is the system controllable?	CO3	5
<b><u>Compulsory:</u></b>				
9.	a.	Comment on the significance of Lyapunov Stability.	CO3	10
	b.	Explain in brief about Lyapunov Stability theorems	CO3	10

ALL THE BEST